# Recitation 2: Value of UI

Jon Cohen

September 24, 2021

# Questions you should be able to answer at the end

- 1. Different approaches use different causal effects. Why do we need one type of elasticity for one approach but not the other?
- 2. Baily-Chetty uses a Taylor expansion but not a comparative static, while Chetty (2008) does the opposite. Why?
- 3. How does each approach deal with state-dependent utility?

# Questions you should be able to answer at the end

- 1. Different approaches use different causal effects. Why do we need one type of elasticity for one approach but not the other?
- 2. Baily-Chetty uses a Taylor expansion but not a comparative static, while Chetty (2008) does the opposite. Why?
- 3. How does each approach deal with state-dependent utility?

Question to ponder afterwards:

- 1. These approaches are for binary losses. What about continuous risks?
- 2. Private insurance value comes from marginal utility. Why might social value depend on utility levels? Anything else?

## Disclaimer: There's a lot of material

- I will prioritize material related to this year's class
- I will mostly skip material from past years' classes and math tools
- But feel free to post on Canvas or come to OH to discuss any of it!

# Recap of Value of UI Approaches

- 1. Causal effect of UE onset (e.g. Gruber '97, Fadlon and Nielsen '19)
- 2. Causal effect of environment (e.g. Chetty '08)
- 3. 1 + 2 + good ol' directly revealed preference! (Landais and Spinnewijn '20)
- 4. Causal effect of UI generosity (e.g. Shimer and Werning '07...not what you read!)

#### Course Theme: Sufficient Statistics

- It's hard (and sometimes not transparent) to recover all "structural" model primitives (e.g. borrowing constraints, time discount rate, adjustment costs, etc.)
- It's easier (and sometimes more transparent) to estimate moments and causal effects
- Conditional on a model, those statistics can be sufficient for welfare analysis

#### Course Theme: Sufficient Statistics

- It's hard (and sometimes not transparent) to recover all "structural" model primitives (e.g. borrowing constraints, time discount rate, adjustment costs, etc.)
- It's easier (and sometimes more transparent) to estimate moments and causal effects
- Conditional on a model, those statistics can be sufficient for welfare analysis
  - Baily-Chetty: Taylor expansion to get causal effect of UE on c
  - Landais and Spinnewijn (2020) MPC approach and Chetty (2006): Differentiate FOC to get causal effect of environment on c or e

#### Outline

#### Causal Effect of Unemployment Onset Approaches

Causal Effect of Environment: Landais and Spinnewijn (2020) MPC Approach

Alternative Landais and Spinnewijn (2020) Approaches

Causal Effect of Environment Approach: Chetty (2008)

Causal Effect of UI Generosity: Shimer and Werning (2007)

# Baily (1978)-Chetty (2006) Formula Recap

- Setup: Social planner allocating consumption in employed and unemployed states subject to (i) govt. budget balance and (ii) unobservable search effort
- Result:  $\frac{u'(c_u)-u'(c_e)}{u'(c_e)} = \epsilon_{1-q,b}$ 
  - At optimum: Marginal benefits (LHS insurance value) = Marginal costs (RHS fiscal externality cost)

# Baily (1978)-Chetty (2006) Formula Recap

- Setup: Social planner allocating consumption in employed and unemployed states subject to (i) govt. budget balance and (ii) unobservable search effort
- Result:  $\frac{u'(c_u)-u'(c_e)}{u'(c_e)} = \epsilon_{1-q,b}$ 
  - At optimum: Marginal benefits (LHS insurance value) = Marginal costs (RHS fiscal externality cost)
- Derivation:
  - 1. Worker's private search effort problem
    - Chooses effort given benefits and taxes
  - 2. Planner's welfare problem s.t. budget balance + worker FOC
    - Chooses benefits and taxes given endogenous effort responses
  - 3. Consumption-based approach: Taylor expansion of MU difference
    - Turns (really hard to know) unobservable MU's into observable c's w/ (easier to know) unobservable  $\gamma$

# Moving Beyond the Consumption-Based Approach

#### • Problems:

- 1. Consumption can be hard to measure
- 2. Imposed CRRA structure w/ risk aversion  $\gamma$  as free parameter
- 3. Ignores higher-order Taylor expansion terms
- 4. Taylor expansion assume MU's are from same function (i.e. no state-dependence)
- Solution: Map models to other estimable elasticities

## Relabeling to Derive an Alternative Method

- Baily-Chetty LHS "value of UI" was an across-state gap in MU: v'(c) u'(c)
  - Taylor expansion turns this into variation in *c* scaled by how much the agent dislikes variation in *c*
- Nothing special in the model about *c* being consumption!

## Relabeling to Derive an Alternative Method

- Baily-Chetty LHS "value of UI" was an across-state gap in MU: v'(c) u'(c)
  - Taylor expansion turns this into variation in *c* scaled by how much the agent dislikes variation in *c*
- Nothing special in the model about *c* being consumption!

**Challenge questions**: What are other observable actions? What would the " $\gamma$ " be? *Hint*: Recall non-financial interpretations of  $x_s$  in Landais and Spinnewijn (2020)

## Relabeling to Derive an Alternative Method

- Baily-Chetty LHS "value of UI" was an across-state gap in MU: v'(c) u'(c)
  - Taylor expansion turns this into variation in c scaled by how much the agent dislikes variation in c
- Nothing special in the model about *c* being consumption!

**Challenge questions**: What are other observable actions? What would the " $\gamma$ " be? *Hint*: Recall non-financial interpretations of  $x_s$  in Landais and Spinnewijn (2020) See Fadlon and Nielsen (2019) JPubEc...and next part!



Causal Effect of Unemployment Onset Approaches

Causal Effect of Environment: Landais and Spinnewijn (2020) MPC Approach

Alternative Landais and Spinnewijn (2020) Approaches

Causal Effect of Environment Approach: Chetty (2008)

Causal Effect of UI Generosity: Shimer and Werning (2007)

Applies general framework to measure value of marginal UI \$ (i.e. across-state MRS) using:

- 1. Standard theory and empirics: consumption drop at UE onset
- 2. Standard theory, novel institutional setting: WTP for supplemental insurance
- 3. Novel theory and empirics: State-specific MPC's

Applies general framework to measure value of marginal UI \$ (i.e. across-state MRS) using:

- 1. Standard theory and empirics: consumption drop at UE onset
- 2. Standard theory, novel institutional setting: WTP for supplemental insurance
- 3. Novel theory and empirics: State-specific MPC's

Intellectual history: Early WP version did not particularly emphasize the MPC approach

### General Framework (Paper Notation)

Max EU given action z to lower UE risk and action xs to change within-state cs for s ∈ {e, u}:

$$V = \pi(z)v_u(c_u, x_u, z) + (1 - \pi(z))v_e(c_e, x_e, z) - z$$

• Consumption given income  $y_s$  and (relative) price  $p_s$  of action  $x_s$  to per unit of  $c_s$ :

$$c_s = y_s + \frac{1}{p_s} x_s$$

# General Framework (Translated to Class Notation)

Simplifying assumptions:

- 1. Exogenous UE risk e (and therefore ignore z)
  - Not important for consumption-based approaches
    - Why not? Why is it important for the revealed preference approach based on supplemental UI contract purchase?
- 2. Additively separable utility  $v_s(c_s) \psi(x_s)$ 
  - Done in paper to ignore cross-partials when differentiating FOC

$$V = e[v_e(c_e) - \psi(x_e)] + (1 - e)[v_u(c_u) - \psi(x_u)] \quad \text{s.t.} \quad c_s = y_s + \frac{1}{p_s}x_s$$

#### 1<sup>st</sup>-order conditions

$$ev'_e(c_e) = \lambda_e \tag{1}$$

$$e\psi'(x_e) = \lambda_e \frac{1}{p_e} \tag{2}$$

$$(1-e)v'_u(c_u) = \lambda_u \tag{3}$$

$$(1-e)\psi'(x_u) = \lambda_u \frac{1}{p_u} \tag{4}$$

Combine (1) and (3) for Baily-Chetty LHS in terms of Lagrange multipliers:

 $v'_u(c_u) - u'(c_e) = (1 - e)\lambda_u - e\lambda_e$  Combine (1) and (2) or (3) and (3) for Econ 101 intuition within-state across-actions:

$$\frac{\partial v_s(c_s)}{\partial c} = p_s \frac{\partial \psi(x_s)}{\partial x}$$

Consider different types of  $x_s$ :

- 1. Spousal labor
- 2. Savings

Consider different types of  $x_s$ :

- 1. Spousal labor
- 2. Savings
- How could we think of  $p_x$  and  $\psi(x_s)$ ?
- Does this get us anywhere useful right away?

#### Making Progress to Observables

$$rac{\partial v_s(c_s)}{\partial c} = p_s rac{\partial \psi(x_s)}{\partial x}$$
 s.t.  $c_s = y_s + rac{1}{p_s} x_s$ 

- Goal: Get MRS  $\frac{v'_u(c_u)}{v'_e(c_e)}$
- Good news: We see  $v'_s(c_s)!$
- Bad news: No clue on what to do with  $p_s$  and  $\psi$
- Strategy:

## Making Progress to Observables

$$rac{\partial v_s(c_s)}{\partial c} = p_s rac{\partial \psi(x_s)}{\partial x}$$
 s.t.  $c_s = y_s + rac{1}{p_s} x_s$ 

- Goal: Get MRS  $\frac{v'_u(c_u)}{v'_e(c_e)}$
- Good news: We see  $v'_s(c_s)!$
- Bad news: No clue on what to do with  $p_s$  and  $\psi$
- Strategy: Get within-state comparative statics w.r.t. wealth  $y_s$ 
  - **Usefulness:** Will substitute out artificial construct  $p_s$  for an estimable elasticity
  - New challenge: Will have 2<sup>nd</sup> derivatives floating around

1. Differentiate FOC w.r.t.  $y_s$  (recall 1<sup>st</sup> reciation slides):

 $\Rightarrow \frac{\mathrm{d}c_s}{\mathrm{d}y_s} = \frac{v' \ast "\mathsf{stuff"}}{v' \ast "\mathsf{things"} + "stuff"}$ 

1. Differentiate FOC w.r.t.  $y_s$  (recall 1<sup>st</sup> reciation slides):

$$\Rightarrow \frac{\mathrm{d}c_s}{\mathrm{d}y_s} = \frac{v' \ast "\mathsf{stuff}"}{v' \ast "\mathsf{things}" + "stuff"}$$

2. Based on above expression, define  $O(MPC_s) \equiv \frac{\frac{\mathrm{d}c_s}{\mathrm{d}y_s}}{1 - \frac{\mathrm{d}c_s}{\mathrm{d}y_s}}$ :  $\Rightarrow v'(c_s) = O(MPC_s) *$  "other stuff"

1. Differentiate FOC w.r.t.  $y_s$  (recall 1<sup>st</sup> reciation slides):

$$\Rightarrow \frac{\mathrm{d}c_s}{\mathrm{d}y_s} = \frac{v' \ast "\mathsf{stuff"}}{v' \ast "\mathsf{things"} + "stuff"}$$

- 2. Based on above expression, define  $O(MPC_s) \equiv \frac{\frac{\mathrm{d}c_s}{\mathrm{d}y_s}}{1 \frac{\mathrm{d}c_s}{\mathrm{d}y_s}}$ :  $\Rightarrow v'(c_s) = O(MPC_s) * \text{"other stuff"}$
- 3. Divide within-state expressions to get MRS:



1. Differentiate FOC w.r.t.  $y_s$  (recall 1<sup>st</sup> reciation slides):

$$\Rightarrow \frac{\mathrm{d}c_s}{\mathrm{d}y_s} = \frac{v' \ast "\mathsf{stuff"}}{v' \ast "\mathsf{things"} + "stuff"}$$

- 2. Based on above expression, define  $O(MPC_s) \equiv \frac{\frac{\mathrm{d}c_s}{\mathrm{d}y_s}}{1 \frac{\mathrm{d}c_s}{\mathrm{d}y_s}}$ :  $\Rightarrow v'(c_s) = O(MPC_s) * \text{"other stuff"}$
- 3. Divide within-state expressions to get MRS:



Intuition check: Low-income people have high MPC's. Does this imply they people have a high value of UI?



Causal Effect of Unemployment Onset Approaches

Causal Effect of Environment: Landais and Spinnewijn (2020) MPC Approach

#### Alternative Landais and Spinnewijn (2020) Approaches

Causal Effect of Environment Approach: Chetty (2008)

Causal Effect of UI Generosity: Shimer and Werning (2007)

### Alternative Approach #1: Consumption Drop

$$MRS \cong 1 + \underbrace{\gamma}_{\text{risk aversion}} (\Delta c)$$

• Standard 2<sup>nd</sup> order Taylor expansion

## Alternative Approach #1: Consumption Drop

$$MRS \cong 1 + \underbrace{\gamma}_{\text{risk aversion}} (\Delta c)$$

- Standard 2<sup>nd</sup> order Taylor expansion
- And rews and Miller (2013) WP notes that  $Cov(\gamma, \Delta c)$  might be important
- Intellectual history aside: WP version emphasized an additional state-dependence term...but relative MU is exactly what we're trying to figure out!

Alternative Approach #2: Revealed Preference Using Supplemental Insurance

- Sweden's labor unions offer the option to purchase supplemental UI
- What better way to assess how people value additional UI than their choices of purchasing additional UI!

## Alternative Approach #2a: Revealed Preference (Bounds)

- At interior optimum, MRS=(probability-weighted) price ratio
- With discrete choice, instead recover bound:

$$MRS \ge (\le) \frac{p_u}{p_e} \frac{1-\pi}{\pi}$$

for buyers (non-buyers) with premium  $p_e$ , benefit  $p_u$ , risk-type  $\pi$ 

- Moral hazard weakens bound when risk type  $\pi$  inferred from risk realizations
- Average the person-specific bounds to get (very loose) bounds on average MRS

Alternative Approach #2b: Revealed Preference (Point Estimates)



- Demographics X is reduced-form way of capturing value of UI
- Exogenous shifters Z<sub>it</sub> that affect risk but not value of UI

Logit regression:  $Choice_{it} = X_{it}\beta - \gamma \tilde{p}(Z_{it}) + \epsilon_{it}$ 

$$MRS = \frac{X_{it}\beta}{\gamma}$$

#### Outline

Causal Effect of Unemployment Onset Approaches

Causal Effect of Environment: Landais and Spinnewijn (2020) MPC Approach

Alternative Landais and Spinnewijn (2020) Approaches

Causal Effect of Environment Approach: Chetty (2008)

Causal Effect of UI Generosity: Shimer and Werning (2007)

# Main Idea of Chetty (2008) JPE

#### Play around with only worker's private search effort FOC: $h'(q) = v(c_e) - u(c_u)$

- Differentiate FOC to get comparative statics (i.e. estimable elasticities)
- Consider impacts of unconditional asset transfer A and conditional UI benefit b on re-employment q
- End up with gap in marginal utilities in terms of elasticities

# Intuition of Mechanics

- We want  $v'(c_e) u'(c_u)$
- An action's FOC reads off the MU of the action compared to its MC
  - Search is a costly action
  - Return to search is gain of moving from unemployment to employment
- Search effort FOC depends on MU of search effort and gap in levels of utility over consumption
- Comparative statics from search FOC get us  $v'(c_e) u'(c_u)$  and estimable elasticities

## Details of Mechanics

Worker objective (same as Baily-Chetty w/ additive separability):

 $qu(c_u) - (1-q)v(c_e) - h(q)$ 

FOC:

$$h'(q) = u(c_u) - v(c_e)$$

• Comparative static on transfer A to **both states**:  $\frac{\partial q}{\partial A} = \{v'(c_e) - u'(c_u)\}/h''(q)$ 

• "Liquidity effect" ( $\leq 0$ , but < 0 only if there's a MU gap)

- Comparative static on transfer b to **unemployed state**:  $\frac{\partial q}{\partial b} = -u'(c_u)/h''(q)$ 
  - "Moral hazard effect" (< 0 by non-satiation)

• Combine comparative statics to get **value of insurance**:  $\frac{v'(c_e)-u'(c_u)}{v'(c_e)} = -\frac{\frac{\partial q}{\partial A}}{\frac{\partial q}{\partial A} - \frac{\partial q}{\partial A}}$ 

• Value  $\geq 0$  (by above signs)

#### Aside: Cramer's Rule!

#### Matrix algebra to make comparative statics easier

- Especially useful with multiple FOC's where multiple margins may adjust
- See David Card's labor notes for a detailed discussion

Suppose you have a system of equations (i.e. totally differentiated FOCs): Ax = b

• Consumer optimization example: x is vector of differentiated endogenous choices, A is bordered Hessian with utility function  $2^{nd}$  derivatives, and b is the matrix of terms with differentiated exogenous parameters

Formula for entry  $x_i$ :

$$x_i = \frac{\det(\mathbf{A}_i)}{\det(\mathbf{A})}$$

where  $\mathbf{A}_i$  replaces column i of  $\mathbf{A}$  with vector  $\mathbf{b}$ 

• Set all but one differentiated parameter = 0 to get comparative static

#### Aside on the Aside: Monotone Comparative Statics!

#### "Differentiate the FOC" when it's not differentiable due to functional form or discreteness

- Signing comparative statics is determined by assumptions on second derivatives/cross-partials
- Economic assumptions aren't really about differentiability
- More general conditions can deliver the same predictions

E.g. Rather than assume  $u(\cdot)$  convex, assume increasing differences:

$$u(x^{H}, y^{H}) - u(x^{L}, y^{H}) \ge u(x^{H}, y^{L}) - u(x^{L}, y^{L})$$

for 
$$x^H > x^L$$
,  $y^H > y^L$ 

Intuition #1: Slutsky Price Theory

$$\frac{v'(c_e)+u'(c_u)}{v'(c_e)} = -\frac{\frac{\partial q}{\partial A}}{\frac{\partial q}{\partial A} - \frac{\partial q}{\partial b}}$$

• Could also get comparative static of **employed wage**:  $\frac{\partial q}{\partial w} = v'(c_e)/h''(q) > 0$ 

- Algebra in the privacy of your own home:  $\underbrace{\frac{\partial q}{\partial b}}_{\text{"uncompensated effect"}} = \underbrace{\frac{\partial q}{\partial A}}_{\text{"income effect"}} - \underbrace{\frac{\partial q}{\partial w}}_{\text{"substitution effect"}}$
- "Income effect" can change behavior, but doing so increases welfare by facilitating q decision that would occur with unconstrained borrowing
- "Substitution effect" changes behavior due tothe wedge between the private and social returns to search effort
- "Income" effects reveal welfare-enhancing smoothing while "substitution" effects reveal welfare-decreasing distortions

#### Intuition #2: Revealed Preference

$$\frac{v'(c_e) - u'(c_u)}{v'(c_e)} = -\frac{\frac{\partial q}{\partial A}}{\frac{\partial q}{\partial A} - \frac{\partial q}{\partial b}}$$

- If it's hard for agent to smooth transitory income shocks, they're stuck exerting a lot of costly search effort
- Agent reveals that that's the case if an unconditional grant changes search similar to a conditional grant
- How much agent chooses to "spend" unconditional transfer on avoiding costly search

#### Intuition #2: Revealed Preference

$$\frac{v'(c_e) - u'(c_u)}{v'(c_e)} = -\frac{\frac{\partial q}{\partial A}}{\frac{\partial q}{\partial A} - \frac{\partial q}{\partial b}}$$

- If it's hard for agent to smooth transitory income shocks, they're stuck exerting a lot of costly search effort
- Agent reveals that that's the case if an unconditional grant changes search similar to a conditional grant
- How much agent chooses to "spend" unconditional transfer on avoiding costly search Intuition check: A friend remarks that the above result is weird; if unemployment is awful, wouldn't we expect them to (1) keep searching hard but (2) still have high UI value?

- (Different from Chetty (2006) JPubEc on the Baily-Chetty formula!)
- 2006 Upshot: Labor supply elasticities can recover risk aversion
- 2006 Intuition: Risk aversion  $\iff$  diminishing  $MU_c$ . And  $MU_c$  mediates LS income effect.

- (Different from Chetty (2006) JPubEc on the Baily-Chetty formula!)
- 2006 Upshot: Labor supply elasticities can recover risk aversion
- 2006 Intuition: Risk aversion  $\iff$  diminishing  $MU_c$ . And  $MU_c$  mediates LS income effect.
  - What happens when your wage increases?
  - Substitution effect > 0, income effect < 0

- (Different from Chetty (2006) JPubEc on the Baily-Chetty formula!)
- 2006 Upshot: Labor supply elasticities can recover risk aversion
- 2006 Intuition: Risk aversion  $\iff$  diminishing  $MU_c$ . And  $MU_c$  mediates LS income effect.
  - What happens when your wage increases?
  - Substitution effect > 0, income effect < 0
  - Risk-averse consumer will have large income effect
    - Increased wage made them richer  $\Rightarrow$  additional consumption doesn't mean as much because  $MU_c$  diminished rapidly

- (Different from Chetty (2006) JPubEc on the Baily-Chetty formula!)
- 2006 Upshot: Labor supply elasticities can recover risk aversion
- 2006 Intuition: Risk aversion  $\iff$  diminishing  $MU_c$ . And  $MU_c$  mediates LS income effect.
  - What happens when your wage increases?
  - Substitution effect > 0, income effect < 0
  - Risk-averse consumer will have large income effect
    - Increased wage made them richer  $\Rightarrow$  additional consumption doesn't mean as much because  $MU_c$  diminished rapidly
- 2008 Mapping: Uninsured, risk-averse agent will have large "income" effect

# Aside: Chetty (2006) AER Details

- Argument above relies on additive separability of labor and consumption  $(u_{cl} = 0)$ 
  - Just as the Baily-Chetty formula relies on additive separability<sup>1</sup>
- If higher consumption makes work less painful ( $u_{cl} > 0$ ), highly risk-averse agents may nevertheless increase hours when wage increases
  - i.e. marginal disutility of labor falls from increased consumption from income effect
  - Idea of estimating complementarity: Estimate consumption changes for consumer who experiences exogenous shock to labor supply (e.g. job loss, disability, etc.)
    - Hard to get causal *point* estimate, so rely on *bounds* (i.e. partial identification)

# Aside: Chetty (2006) AER Graphical Intuition In Pictures



# Aside: Chetty (2006) AER Graphical Intuition In Words (for last slide)

- x-axis: labor, y-axis: marginal utilities
- Downward-sloping line: Diminishing marginal utility of c
- Upward-sloping line: Increasing marginal disutility of *l*
- Intersection: FOC equality
- Initial LS  $l_0$  at wage  $w_0$
- After the wage increases to  $w_1 > w_0...$ 
  - LS increases to  $l_A$  for CRRA parameter  $\gamma < 1$  (i.e.  $\downarrow$  risk aversion  $\rightarrow \downarrow$  income effect)
  - LS increases to  $l_A$  for CRRA parameter  $\gamma > 1$  (i.e.  $\uparrow$  risk aversion  $\rightarrow \uparrow$  income effect)
  - Income and substitution effects cancel out for  $\gamma = 1$  (i.e. log utility)!
  - If  $u_{cl} \neq 0$ , the marginal disutility of l line also shifts when w increases
    - Drawn graph implicitly assumes  $u_{cl} > 0$  because shaded is a downward shift

## Aside: Exercise for the Very Ambitious Student

Gain a deeper understanding of the relationship between risk aversion, labor supply elasticity, and labor-consumption complementarity

- 1. Set up a Frisch consumption-leisure maximization (i.e. treating the Lagrange multiplier on income  $\lambda$  as a fixed parameter)
- 2. Use Cramer's Rule (!!!) to get comparative statics for consumption and leisure (w.r.t. parameters: wage w, non-labor income y, and  $\lambda$ )
- 3. Log-linearize Frisch demands for consumption and leisure (w.r.t parameters)
- 4. Relate the expressions from steps (2) and (3)

See David Card's labor lecture notes for more detail

# Aside: Reconciling Chetty (2006) AER and Chetty (2008) JPE

- **Peter:** Interesting that labor supply paper delivering relatively low risk aversion estimate  $(\gamma \approx 1)$  but UI paper delivers relatively high insurance value estimate  $(RR^* > 50\%)$
- **Me:** Chetty (2012) ECMA suggests optimization frictions attenuate labor supply elasticity estimates

#### Outline

Causal Effect of Unemployment Onset Approaches

Causal Effect of Environment: Landais and Spinnewijn (2020) MPC Approach

Alternative Landais and Spinnewijn (2020) Approaches

Causal Effect of Environment Approach: Chetty (2008)

Causal Effect of UI Generosity: Shimer and Werning (2007)

#### Overview of Method

- (Not Shimer and Werning (2008) AER on a structural model of liquidity vs. insurance!)
- Worker's utility is monotonically increasing in the after-tax wage w

   → After-tax reservation wage of the unemployed is a sufficient statistic for welfare
   ⇒ Sign of dw

   → After-tax reservation wage of the unemployed is a sufficient statistic for welfare
   ⇒ Sign of dw

   → After-tax reservation wage of the unemployed is a sufficient statistic for welfare
   ⇒ Sign of dw

   → After-tax reservation wage of the unemployed is a sufficient statistic for welfare
   ⇒ Sign of dw

   → After-tax reservation wage of the unemployed is a sufficient statistic for welfare
   ⇒ Sign of dw

#### Main Intuition

- Worker reveals the net value of increased benefits that will be financed by taxes
- Increase in pre-tax reservation wage  $\bar{w}$  captures "gross value" of UI, while increase in tax  $\tau$  captures "gross cost" of UI
  - Analogous to LHS and RHS of Baily-Chetty formula

#### Why After-Tax?

- Of course  $\bar{w}$  increases with b!
- But that also comes with a tax increase that they have to pay for
- Whether they value the UI more than the actuarially fair cost (which includes any behavioral response) determines whether an expansion raises or lowers the *after-tax* reservation wage

#### Preliminaries

- Reservation wage  $\bar{w}$  is lowest wage sequential searcher willing to accept
  - Defined as fixed point (McCall 1970)
  - Accept job offer and work forever (for simplicity, can be relaxed)
- Budget-balanced UI benefits b financed by tax au

$$\underbrace{U(\bar{w} - \tau)}_{\text{after-tax res. wage}} = \underbrace{U(b)}_{\text{UI}} + \underbrace{\alpha}_{\text{PV term arrival rate}} \underbrace{\lambda}_{\bar{w}} \underbrace{\int_{\bar{w}}^{\infty} \underbrace{[U(w) - U(\bar{w})]}_{\text{gain from job offer}} \underbrace{dF(w)}_{\text{offer distr.}}$$

Worker indifferent between remaining unemployed and working at w
 ⇒ lifetime utility V = U(w̄-τ)/ρ (discount rate ρ)

 This is the key equation!

# My Personal Views on Shimer-Werning After-Tax Test

- 1. Requires an unreasonable amount of worker sophistication in job search strategies
  - Paper's response: Can elicit the pre-tax reservation wage and have the researcher use estimated moral hazard effects to recover the effect on the post-tax reservation wage
- 2. Requires unreasonable sophistication in self-reports
  - I believe consumers do implicit optimization to get close to MRS=price ratio, but I wouldn't trust someone's self report of their MRS between two goods
  - Paper's response: We motivate advancing reservation wage elicitation methods

# Satisfying Properties

- Super clever!
- Theoretically robust
- Doesn't require parametric assumptions
- Doesn't require administrative data
- Can be used to study the value of **any** policy to help the unemployed